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# The Physics of Fusion Energy: Why We (Probably) Can't Make a Reactor on the Head of a Pin

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# The Physics of Fusion Energy: Why We (Probably) Can't Make a Reactor on the Head of a Pin

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**Invited Tutorial Talk**

**Innovative Confinement  
Concepts Workshop**

***University of Wisconsin,  
Madison WI  
May 27, 2004***

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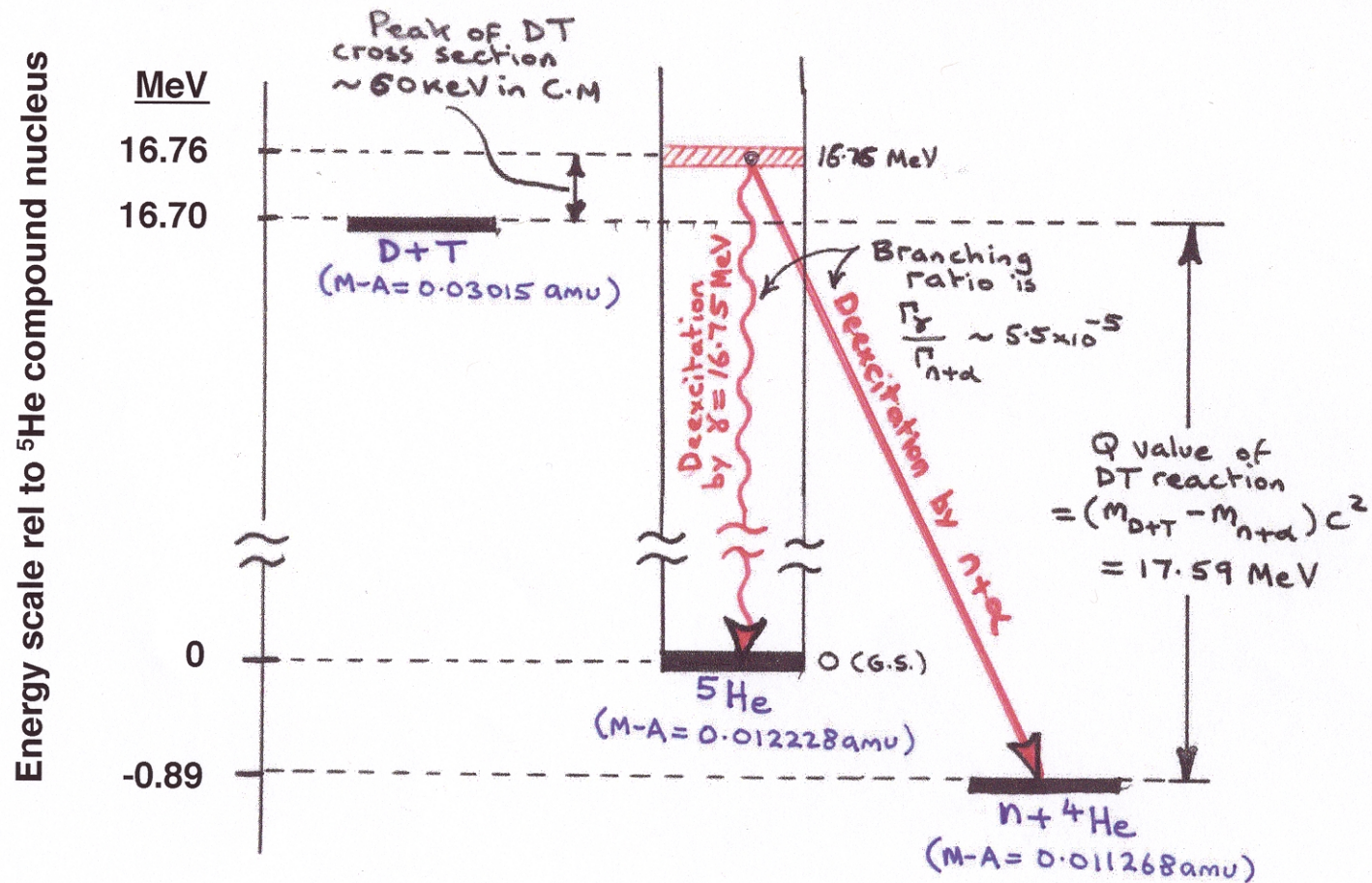
## Some Candidate Fusion Fuels



			<σ.V> at:	
			<u>20keV</u>	<u>200keV</u>
<b>Conventional (and it's still hard!):</b>				
$D + T$	$\rightarrow n + {}^4\text{He}$	+ 17.6Mev	4.2	6.3
<b>Advanced fuels:</b>				
$D + D$	$\rightarrow n + {}^3\text{He}$	+ 3.3Mev	0.0052	0.88
	$\rightarrow p + T$	+ 4.0Mev		
$D + {}^3\text{He}$	$\rightarrow p + {}^4\text{He}$	+ 18.4Mev	0.0038	2.4
<b>You'll also get:</b>				
$T + T$	$\rightarrow n + n + {}^4\text{He}$	+ 11.3Mev	0.0025	0.42
${}^3\text{He} + {}^3\text{He}$	$\rightarrow p + p + {}^4\text{He}$	+ 12.9Mev	0.0001	0.03
$T + {}^3\text{He}$	$\rightarrow n + p + {}^4\text{He}$	+ 12.1Mev	0.003	0.92
$n + X$ (important for high ρ-R ICF targets)				
<b>And if you think this is too easy.....:</b>				
$p + {}^{11}\text{B}$	$\rightarrow {}^4\text{He} + {}^4\text{He} + {}^4\text{He}$	+ 8.7Mev	0.0008	2.4
$p + {}^7\text{Li}$	$\rightarrow {}^4\text{He} + {}^4\text{He}$	+ 17.3Mev	comparable	
$p + {}^9\text{Be}$	$\rightarrow {}^4\text{He} + {}^6\text{Li}$	+ 2.1Mev	comparable	



# Nuclear Energetics of the D-T Reaction





# The Fusion Cross Section – and the Economics of (Thermonuclear) Fusion Energy – is Dominated by the Coulomb Barrier



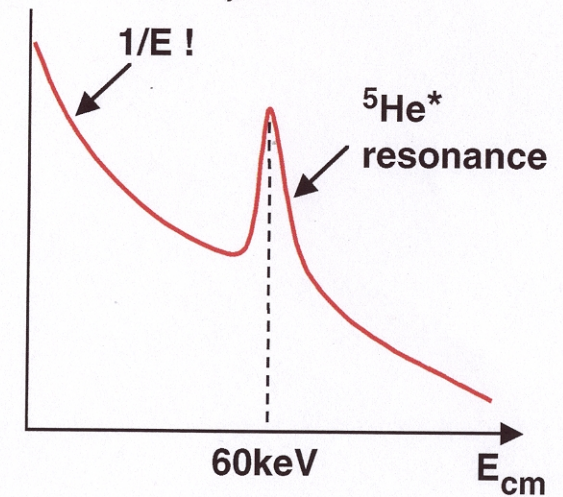
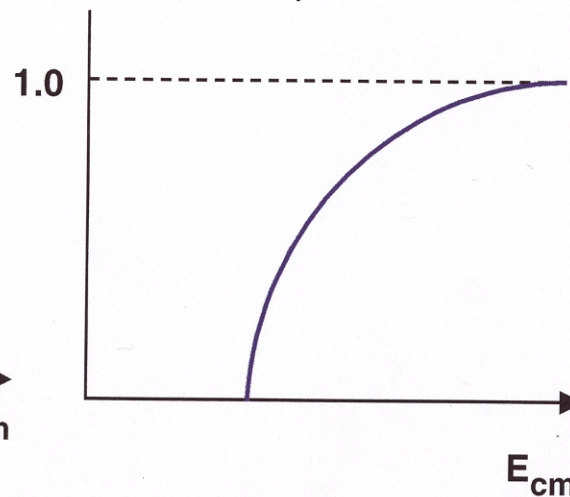
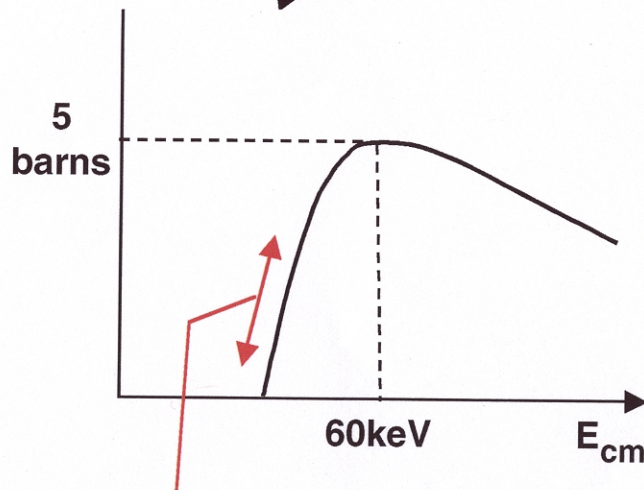
$\sigma(E_{\text{cm}})$

=

prob of Coulomb  
barrier penetration

×

nuclear part



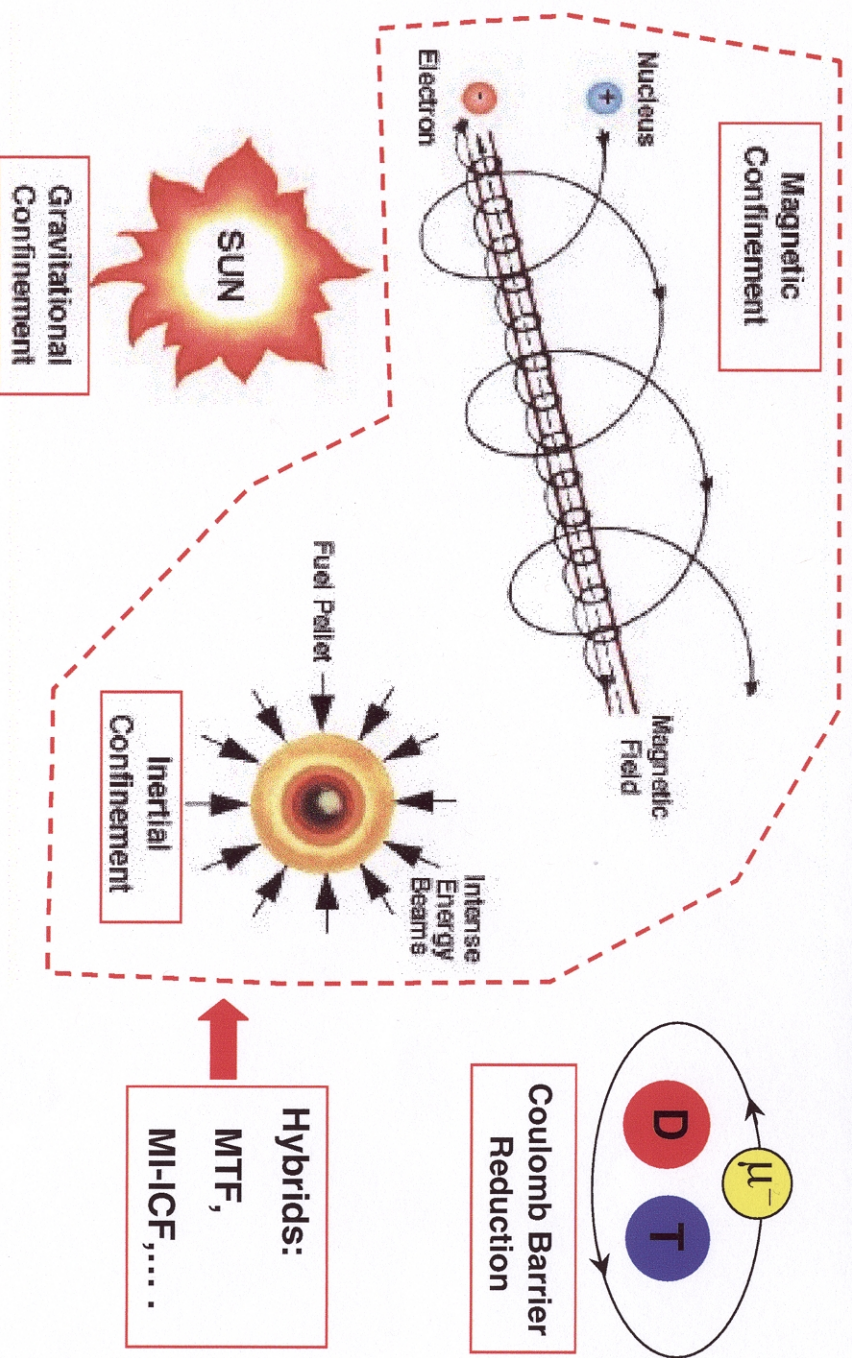
NB: The DT cross section falls ~8 orders of magnitude as energy is reduced from 10keV to 1keV!



# There are Three (and Maybe More...)



## Ways to Achieve Fusion



### Density      Temperature      Confinement Time

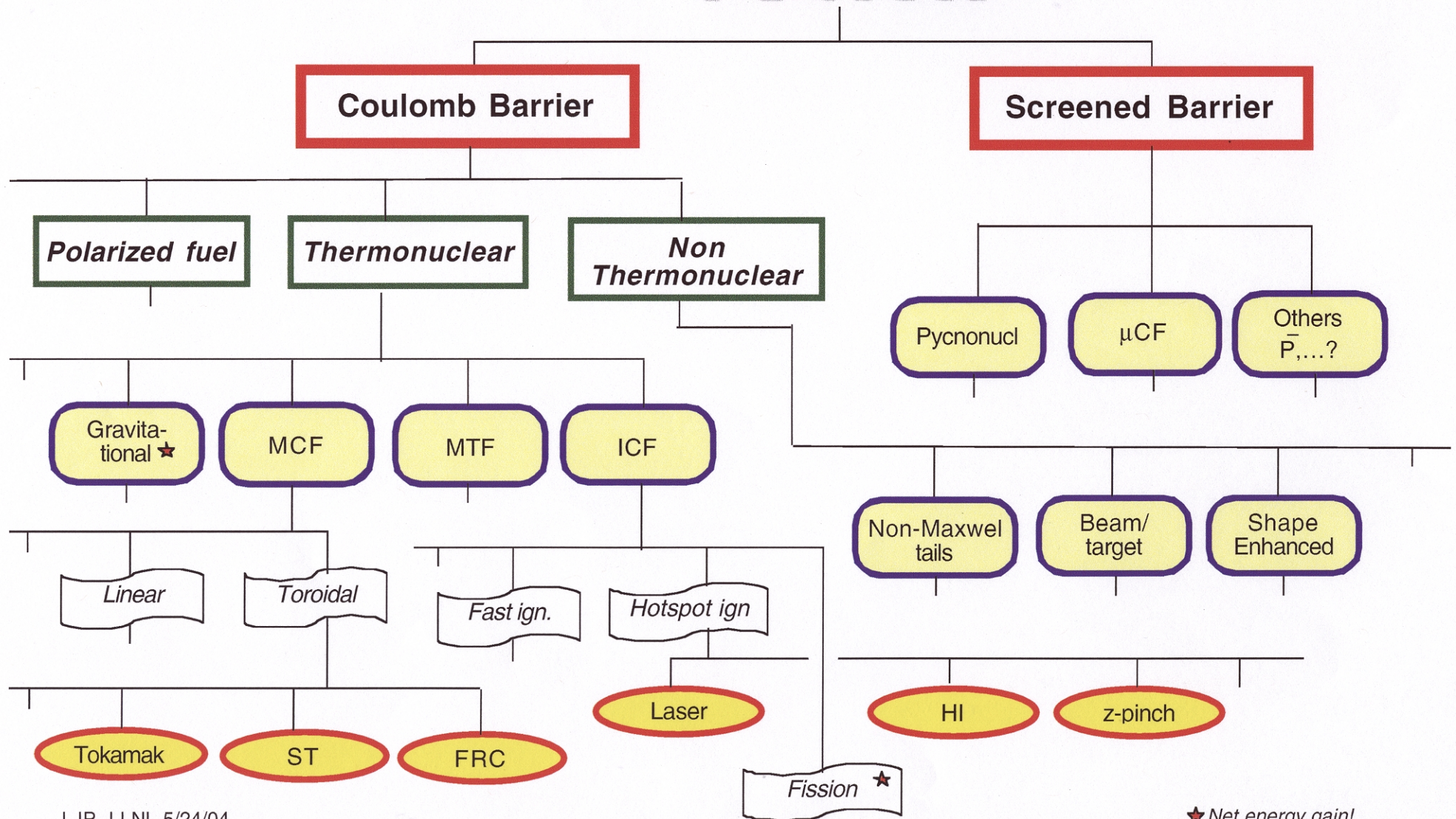
<b>Magnetic</b>	solid/ $10^8$	10keV	seconds
<b>Inertial</b>	$10^3 \times$ solid	10keV (t=0)	10's picoseconds
<b>Gravitational</b>	$10^4 \times$ solid	1keV	$10^5$ years
<b>Coulomb Barrier Reduction</b>	solid	100's °C	Not applicable



# How ( $\Rightarrow$ net energy gain) ?

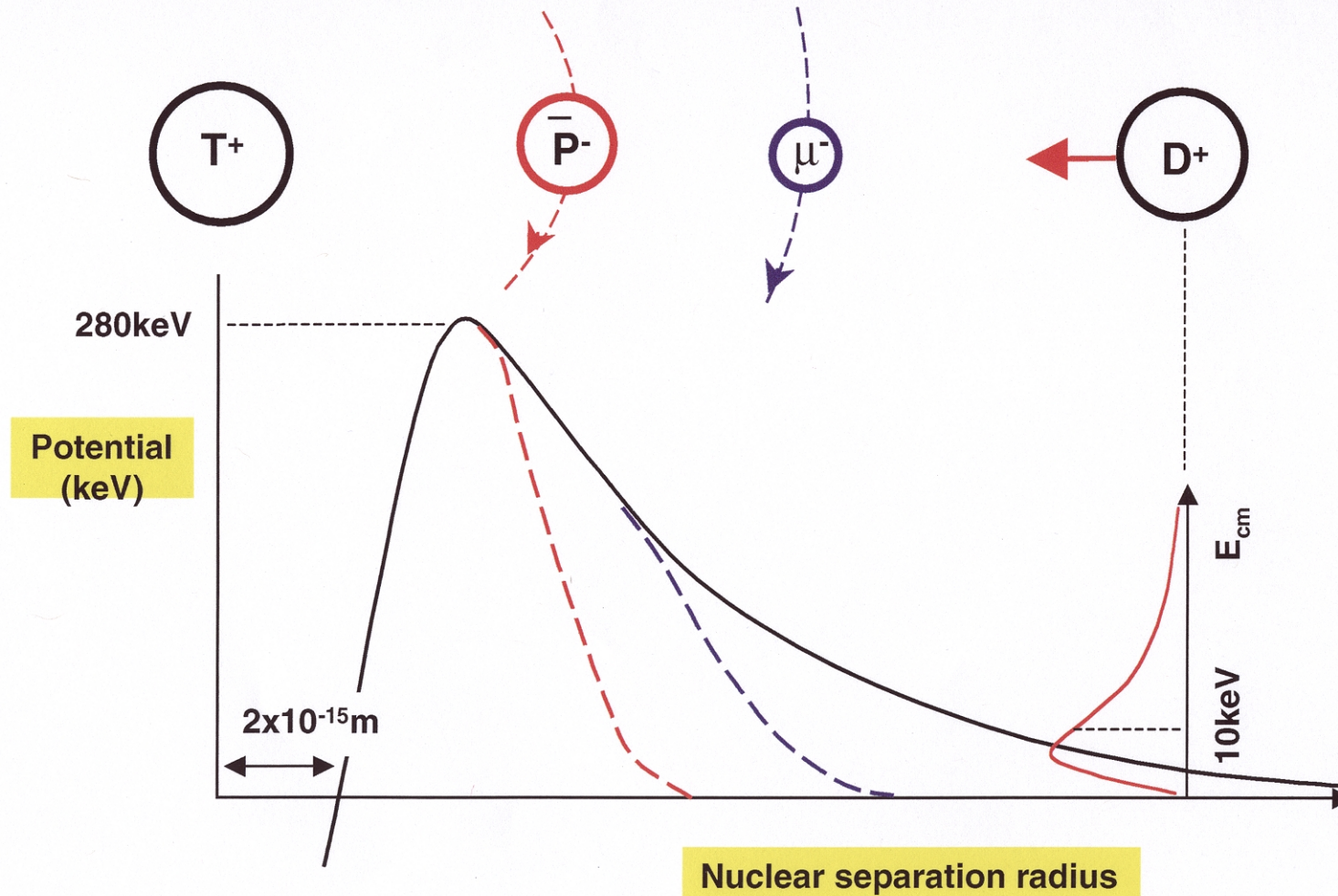


## FUSION



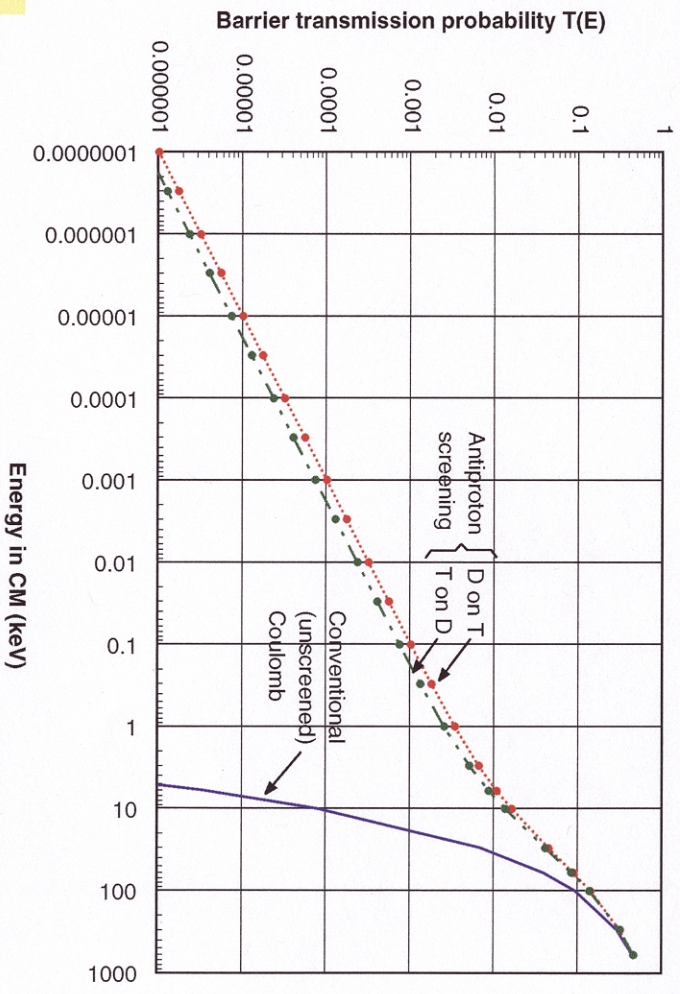


# The Fusion Cross Section is Dominated by Coulomb Barrier Penetration



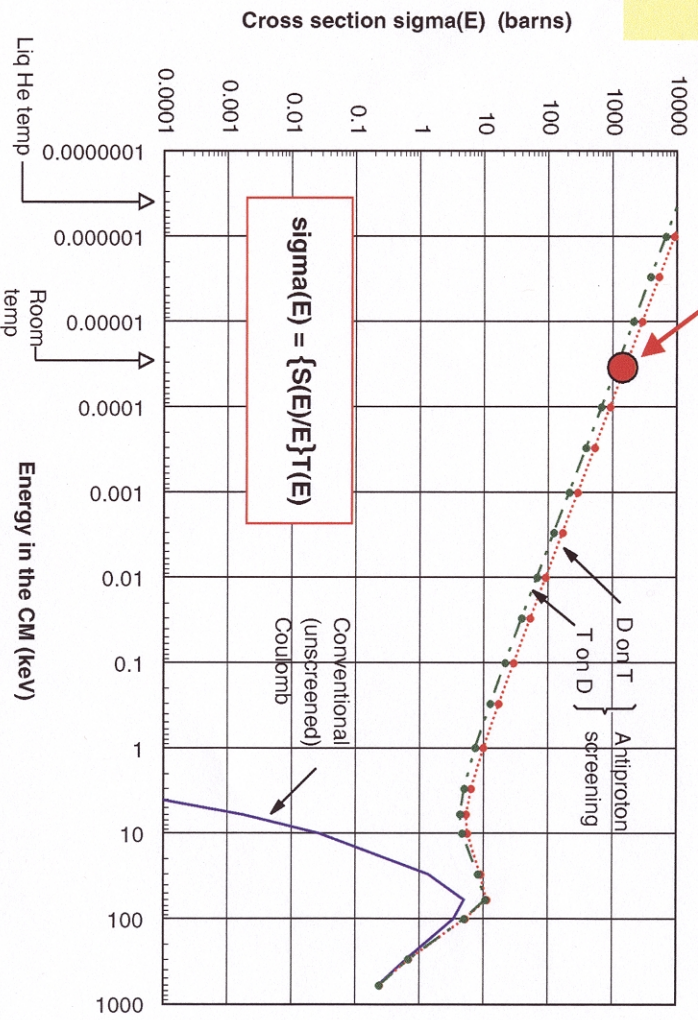


# Modifying the Coulomb Barrier has a Dramatic Effect on Fusion Cross Section



DT fusion cross section at room temperature is  $\sim 1000b$ ! (twice the  $^{235}\text{U}$  fission cross section)

DT FUSION REACTION: BARRIER TRANSMISSION PROBABILITIES FOR CONVENTIONAL (UNSCREENED) COULOMB POTENTIAL AND ANTIPROTON SCREENING



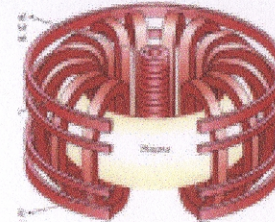
DT FUSION REACTION: CROSS SECTION INCREASE VIA ANTIPROTON SCREENING. THE  $1/E$  TERM DOMINATES THE TRANSMISSION PROBABILITY AT LOW ENERGY



# The Modus Operandi of Magnetic Fusion (Physics) Research



- Find a magnetic topology that holds a plasma in equilibrium



$$\nabla p = \mathbf{j} \times \mathbf{B}$$

- That is stable at desired operating pressures

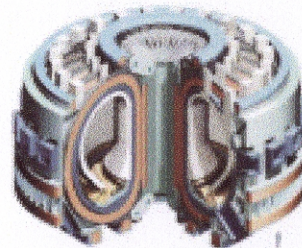
$$\beta = 2\mu_0 p / B^2 \sim \beta_N I / aB, \quad q \sim a^2 B / R I, \dots$$

- That contains heat for a sufficient time to produce net energy gain

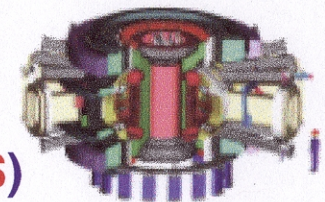
$$P_\alpha + P_{\text{aux}} = E_{\text{th}} / \tau_E + P_{\text{rad}}, \quad Q = P_{\text{fus}} / P_{\text{aux}} \geq 10 \text{ (20)}$$

$$\Rightarrow n \tau_E T \sim \text{few} \times 10^{15} \text{ cm}^{-3} \text{s}^{-1} \text{keV}$$

- For a sufficient burn time

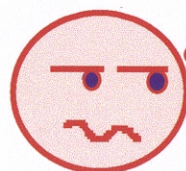


ITER (~400s \$\$\$\$\$)



FIRE (~10s, \$\$)

- But, in any event:

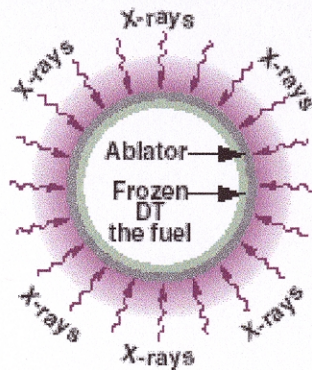


$$T \geq 100,000,000^\circ\text{C}$$

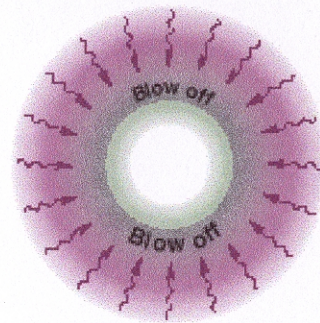
and losses scale as  
~T, T<sup>2</sup>, T<sup>1/2</sup>, ∇T...



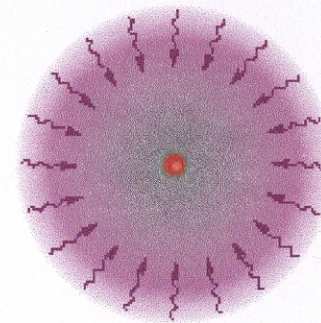
# The Modus Operandi of Inertial Confinement Fusion (Physics) Research



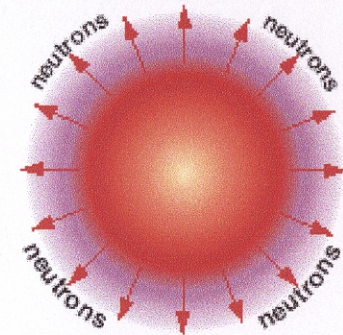
X-rays or driver beams heat ablator



Rocket reaction implodes fuel shell

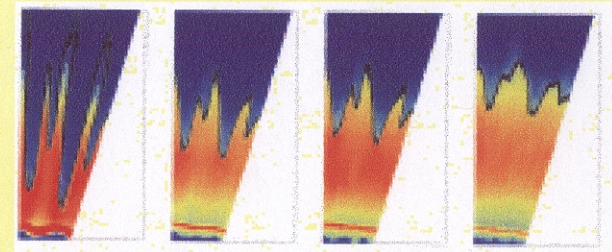


Fuel shell stagnates. Ignition begins in central hotspot



Burn propagates to compressed outer fuel  
Yield is produced

- Ignition and propagating burn:  
 $(\rho R \cdot T)_{\text{hotspot}} \sim 0.3 \text{g.cm}^{-2} \cdot 10 \text{keV}$
- Yield and gain:  
 $(\rho R)_{\text{cold fuel}} \sim 3 \text{g.cm}^{-2}$
- Why we need compression:  
If  $\rho = 0.25 \text{g.cm}^{-3}$ ,  $m = 2.5 \text{kg}$ ,  $Y \sim 70 \text{kt}$ ,  $E_{\text{driver}} \sim 3 \text{GJ}$   
If  $\rho = 400 \text{g.cm}^{-3}$ ,  $m = 5 \text{mg}$ ,  $Y \sim 500 \text{MJ}$ ,  $E_{\text{driver}} \sim 1 \text{MJ}$



But it's all about the symmetry and stability!



# Technology (and Humanity's) Constraints



●  $Q_{\text{eng}} = P_{\text{elec}} / P_{\text{recirc}} = \eta_{\text{th}} P_{\text{fus}} / (P_{\text{aux}} / \eta_{\text{aux}}) = \eta_{\text{th}} \eta_{\text{aux}} Q \geq 3 \text{ (at least!)}$

**MFE:**  $\eta_{\text{th}} \eta_{\text{aux}} Q \geq 3$ ;  $\eta_{\text{th}} \sim 0.3$ ,  $\eta_{\text{aux}} \sim 0.5$ ;  $\Rightarrow Q \geq 20$

**IFE:**  $\eta_{\text{th}} \eta_{\text{driver}} G \geq 3$ ;  $\eta_{\text{th}} \sim 0.3$ ,  $\eta_{\text{driver}} \sim 0.1$ ;  $\Rightarrow G \geq 100$

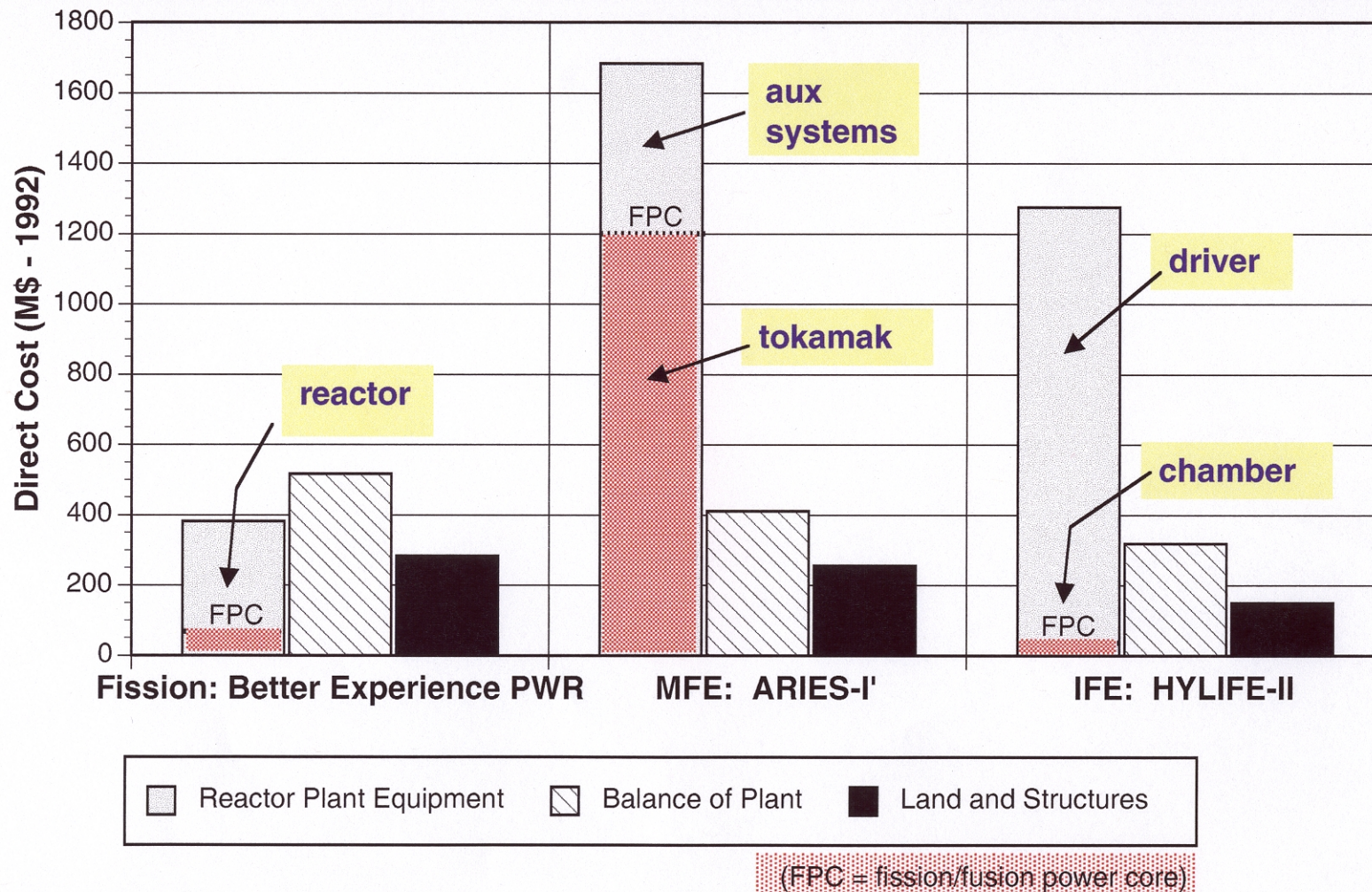
Technology	
Shielding (nuclear cross sections)	$\Rightarrow$ Radial builds, materials
Surface heat flux; volumetric heat removal	$\Rightarrow$ Fusion power density, geometry, radial builds
Radiation damage	$\Rightarrow$ Radial builds, materials
Stresses	$\Rightarrow$ Magnet radial builds
Space charge, optics damage, beam access	$\Rightarrow$ Driver power densities, pulse compression,
Pulsed fatigue	$\Rightarrow$ Radial builds, materials, quality control

"Economics"	
Size / mass / cost	$\Rightarrow$ "Power density" of <b>MFE core</b> or <b>IFE driver</b>
Complexity	$\Rightarrow$ No. of systems, reliability, maintainability
Safety	$\Rightarrow$ Fusion power density, material choices, complexity
Environment (waste disposal)	$\Rightarrow$ Material choices, complexity
Proliferation	$\Rightarrow$ Fuel cycle, materials

**NB: ICF is doing it once; IFE is doing it ten times a second for 30-y at 90% availability!**



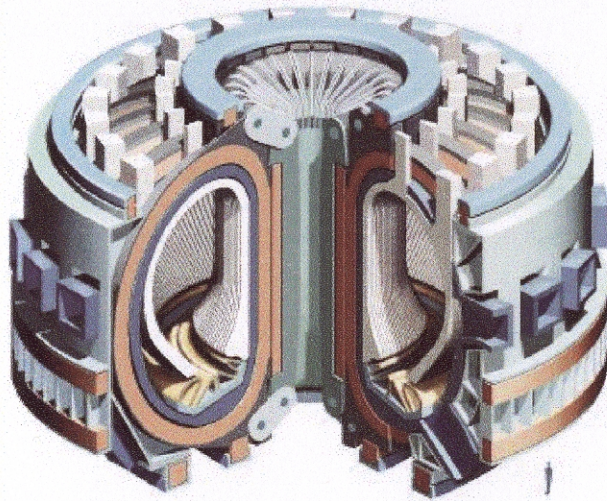
# Capital Costs: Fission -v- Fusion



- ⇒ For MFE, the cost and complexity is in the fusion power core
- ⇒ For IFE, the cost and complexity is in the driver

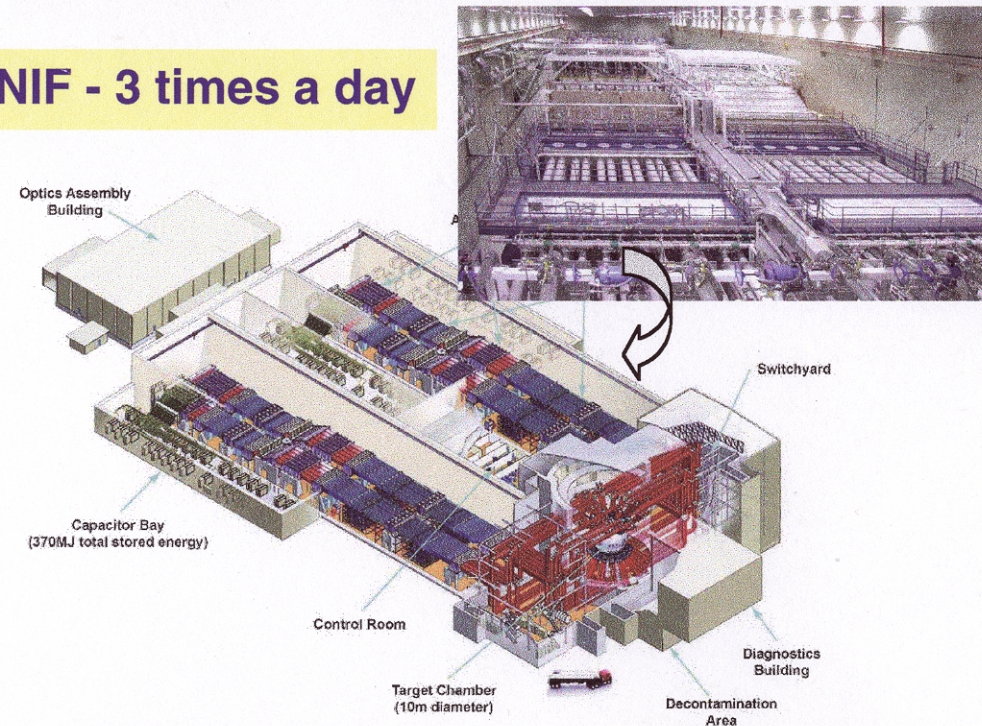


# Present Fusion Systems are Very Complex (But, hey -- we're just trying to make it work at all !)



● ITER - 400secs

● NIF - 3 times a day



Fuel power density ( $\text{MW}/\text{m}^3$ )  
 Fuel power flux ( $\text{MW}/\text{m}^2$ )  
 Fast neutron power flux ( $\text{MW}/\text{m}^2$ )  
 Core power density ( $\text{MW}/\text{m}^3$ )  
 Core mass (tonne)  
 Mass power density ( $\text{kW}_e/\text{tonne}$ )  
 Rel. no. of pipes, welds, pumps, valves....

## Fission (ALWR)

250  
 0.5  
 0.01 (2MeV)  
 10  
 500  
 1000  
 1

## Fusion (ARIES-RS)

5  
 5  
 4 (14MeV)  
 1  
 8,000  
 100  
 ~10



# MFE: Reduce the Size, Cost and Complexity of the Fusion Power Core (Duh!)

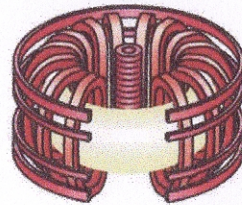


Stellarator



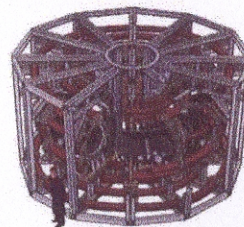
3-D coils

Tokamak



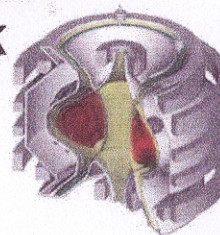
Planar coils,  
with nested sets

RFP



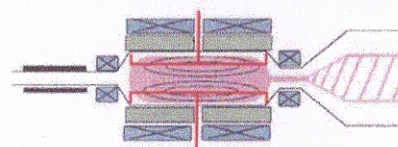
Low-field  
external coils

Spheromak



No toroidal  
coils

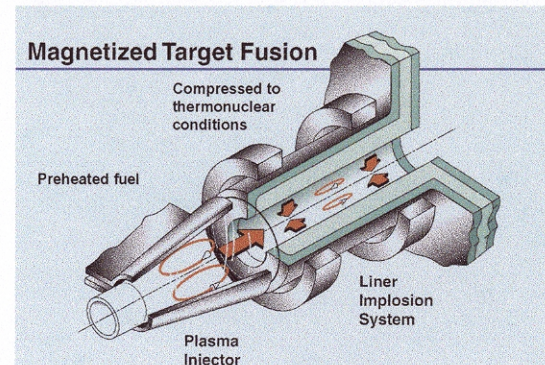
FRC



No toroidal  
field

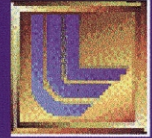
But will it hold  
heat?

( $T \geq 100,000,000^\circ\text{C}$ )



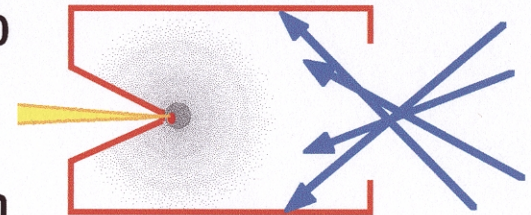


# In IFE, the Target Drives the Driver Requirements ⇒ Advanced Target Concepts?

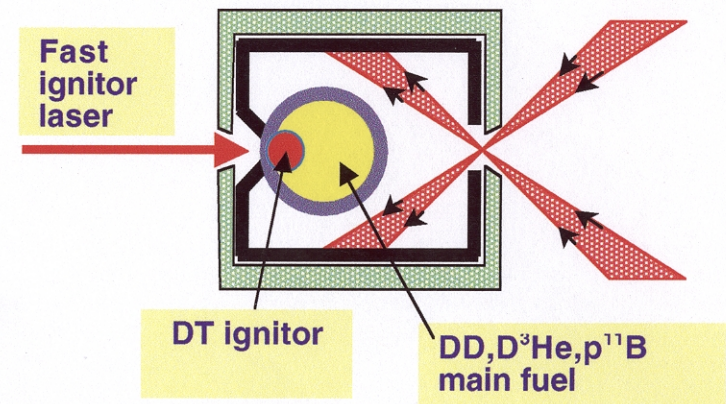


## ■ Fast ignition –

- ❑ Laser fast ignition – Point designs indicates gain ~350 for ~700kJ compression energy and ~100kJ fast ignitor
- ❑ Cone focus geometries are under study
- ❑ High-intensity laser-driven fast ions may be an alternative fast ignition option
- ❑ In general, fast ignition may considerably relax present constraints on timing, symmetry, stability and target fabrication



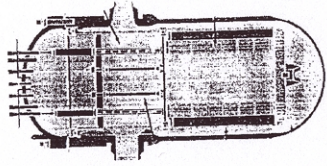
- ## ■ Advanced fuel targets –
- Fast ignition may permit us to burn advanced fuels: D-D/D-<sup>3</sup>He/p-<sup>11</sup>B capsules with 1% DT ignitors. With 0-20% of the energy in fast neutrons, this might permit direct energy conversion of target output.



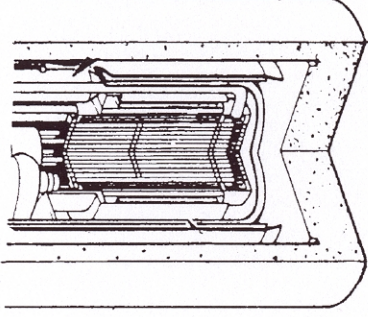
## ■ Can magnetic fields be employed?

- ❑ Z-pinches
- ❑ Magnetized targets – pre-emplaced B-fields may aid hot-spot burn and suppress electron heat conduction



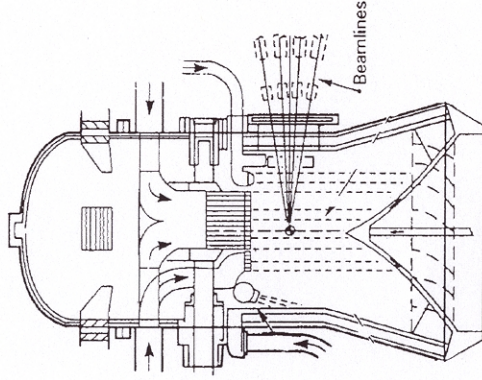


Westinghouse AP600  
(600MW<sub>e</sub> unit)

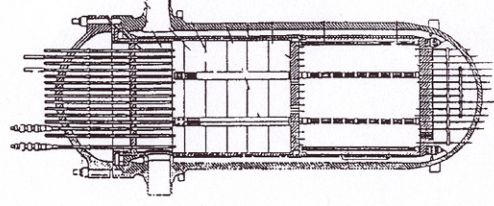


GE ALMR PRISM  
(~300MW<sub>e</sub> unit)

0 1 2 3  
m



HYLIFE-II IFE  
(1000MW<sub>e</sub> unit)

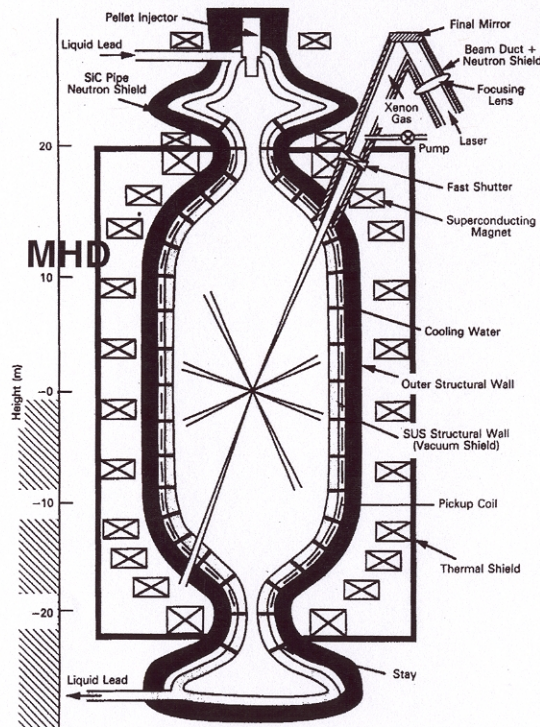


Westinghouse APWR 1300  
(1300MW<sub>e</sub> unit)

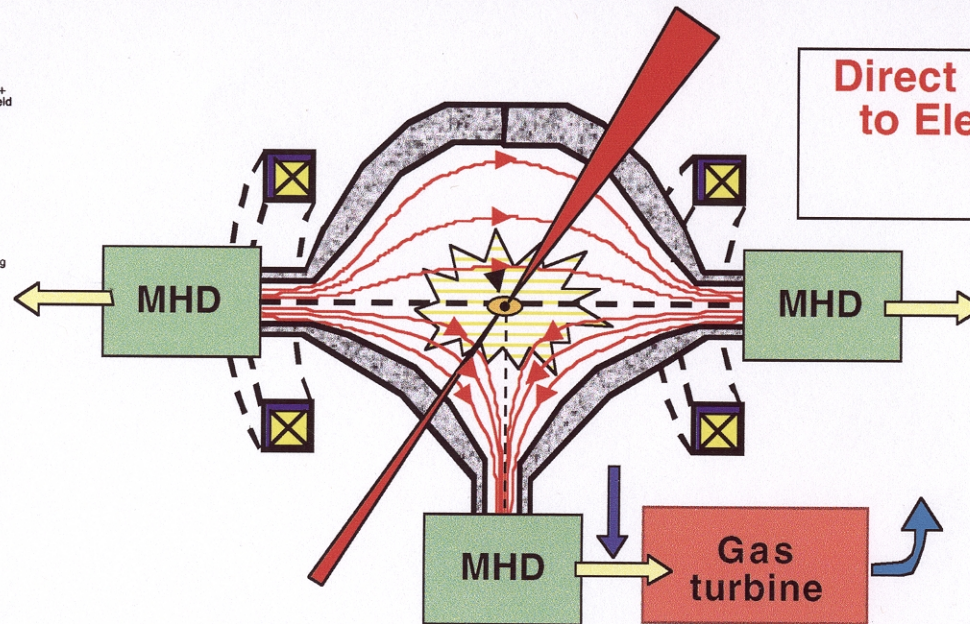
**The IFE Reactor Chamber Is Similar in Size,  
Cost and Complexity to a Fission Reactor  
(to scale)**



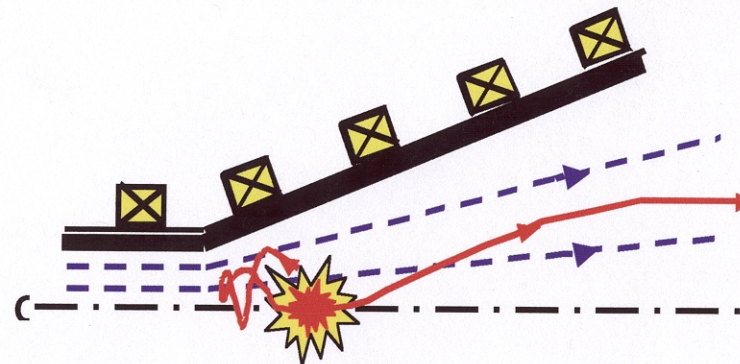
# With Fusion Energy Appearing as Charged Particles (Plasma), We Could.....



**Direct Conversion  
to Electricity via  
Flux Compression  
(Mima et al)**



**Direct Conversion  
to Electricity via  
MHD**



**Directed  
Thrust for  
Advanced  
Space  
Propulsion**

⇒ Can we do more with fusion energy than boil water for a steam cycle?



# 1000MW<sub>e</sub> "MFE" REACTORS: THE IMPACT OF ULTIMATE PHYSICS

	Pulsed Inductive Tokamak <sup>(d)</sup> <i>ITER-like phys.<sup>(a)</sup></i>	Steady-State Advanced Tokamak <i>Advanced, TPX or ARIES-like phys.<sup>(b)</sup></i>	Neoclassical Tokamak <i>Neoclass <math>\tau_E</math>, <math>\beta \leq 1</math></i>	Magnetic Toroid <i>No <math>\tau_E</math>, <math>\beta \leq 1</math></i>	Ultimate Reactor <sup>(c)</sup> <i>No physics constraints</i>
<b>Relative COE</b>	<b>2.4 – 3.3</b>	<b>1.8</b>	<b>1.4</b>	<b>1.2</b>	<b>1.0</b>
Mass power density (kW <sub>e</sub> /tn)	19 - 26	62	100	210	410
<b>Reactor Plant Equip. fract.</b>	<b>0.69– 0.75</b>	<b>0.63</b>	<b>0.55</b>	<b>0.43</b>	<b>0.34</b>
R <sub>0</sub> (m)	9.0 – 11	5.7	4.2	3.8	1.6 <sup>(c)</sup>
A	3.7 – 4.9	3.5	3.5	6.7	1.0*
I (MA)	18 – 15	11	8.0	N/A	N/A
B (T)	6.3 – 7.3	5.9	4.5	2.8	N/A
q <sub>95</sub>	3.0* – 3.0*	4.0*	3.0*	N/A	N/A
P <sub>aux</sub> (MW)	0 – 0	104	0	N/A	N/A
B.S. fract.	0.26 – 0.31	0.71	1.0*	N/A	N/A
Confinement H used	2.0* – 2.0*	2.72	N/A [5.2 <sup>(f)</sup> ]	N/A	N/A
Troy. Coef. $\beta_N$ used	2.5* – 3.0* (d)	6*	N/A [10 <sup>(f)</sup> ]	N/A	N/A
$\beta$ (%)	0.029 – 0.023	0.069	0.15	1.0*	N/A
Neut. wall load (MW/m <sup>2</sup> )	1.6 – 1.2	3.5	5.9	12	13
Burn pulse length(hr)	1 – 10 <sup>(d)</sup>	S. State	S. State	S. State	S. State

\* -- Parameter at constraint bound or fixed. (a) Modest physics ( $H \leq 2$ , range reflects sensitivity to  $\beta_N \leq 2.5 - 3$ , and 1 – 10hr burn).









(b) Advanced physics ( $H \leq 4$ ,  $\beta_N \leq 6$ , s-state) expected from successful TPX program. (c) Can be equally considered point source plasma with a spherical FW radius at  $3.75 + 0.15(s.o) = 3.9m$  to keep optimum neut. wall load at  $\sim 13MW/m^2$  (optimum due to from blanket changeout costs). Note this is also the ultimate ICF reactor ( $\infty$ -rep rate). (d) Cases shown for inductive burn times in the range 1 – 10hr. The ARIES/PULSAR team (Sept 93) suggest optimum pulse length is  $\sim 3hr$ , implying  $\sim 70,000$  pulse fatigue cycles at end-of-life. A 10hr pulse length machine accrues  $\sim 20,000$  pulse fatigue cycles. (f) H or  $\beta_N$  not constrained here but can be backed out from the solution point from other design variables.



# Fusion Energy Beats Advanced Fission in Five Critical Areas.



⇒ **Advanced Physics Solutions Must be Sought for the Remaining Areas**

Fusion -v- Advanced Fission	
<i>Safety and Environment</i>	
<i>Waste Disposal</i>	
<i>Non-Proliferation</i>	
<i>Fuel Cycle</i>	
<i>Advanced energy conversion potential</i>	
<i>Capital Cost</i>	
<i>Complexity and Reliability</i>	
<i>Development Path</i>	
<i>Unit Size</i>	